

# Consistency of Task-Based Authorization Constraints in Workflow System

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# Introduction

- Workflow: consists a collection of tasks that are organized to facilitate some business process specification
  - Purchase order processing
  - Processing tax refunds

# Introduction

- Security Challenge
  - Administration of security-relevant information
  - Specification of authorization policies and constraints
  - Solution
    - RBAC
    - Constraints

# Introduction

- Constraints: restriction on the authorization
  - Separation of Duty
  - Binding of Duties
- Challenge for constraints in workflow system
  - Consistency

# Goal

- Help workflow designers to define a sound constrained workflow authorization schema such that
  - each workflow instance can complete
  - each user or role authorized to perform a task will have an opportunity to perform that task in some workflow instance

# Related Work

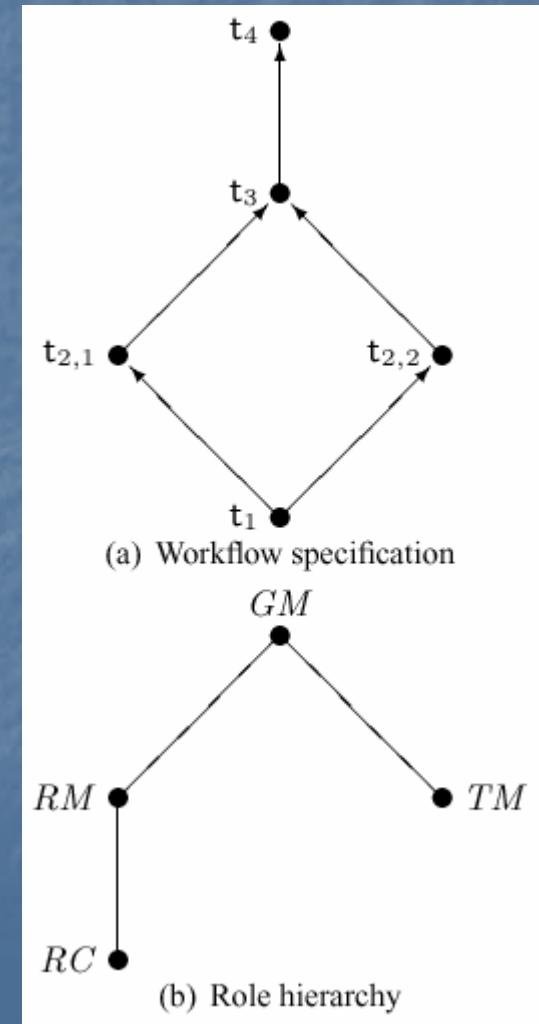
- E. Bertino, E. Ferrari, V. Atluri: TISS 99
  - Role planning and user planning
    - + Constraints are consistent
    - Complicated
- J. Wainer, P. Barthelmess, A. Kumar: IJCIS 03
  - Override constraints when workflow can not be completed
    - + Completing workflow instance
    - Weaken security

# Our Contribution

- Give explicit definition of constraint workflow authorization schema
- Develop simple specification of authorization constraints
- Define consistency rules which can be checked efficiently

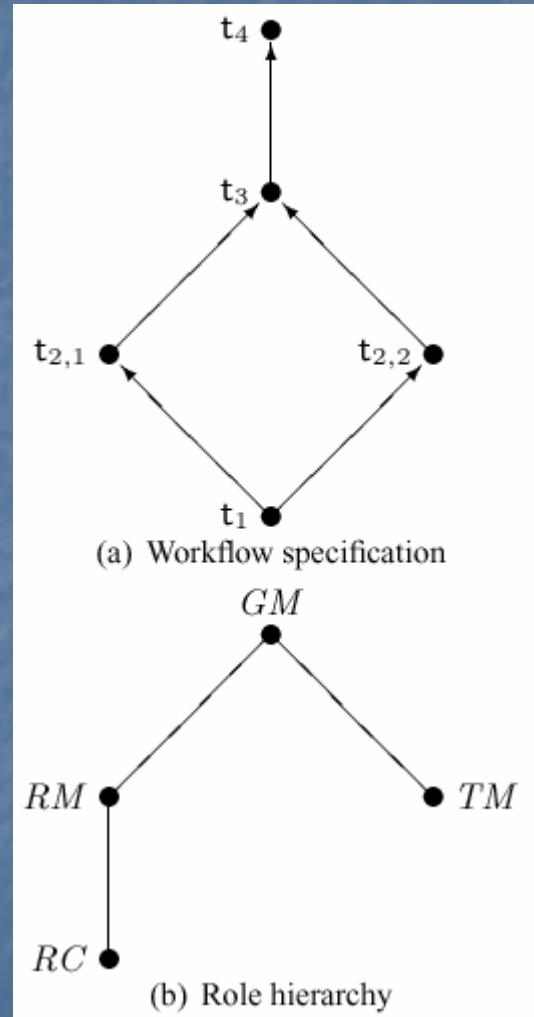
# Workflow Example

- Producing payments for tax refunds
  - $t_1$ : a clerk prepares a check for a tax refund
  - $t_2$ : the check is approved or denied by two different managers
  - $t_3$ : A third manager makes a final decision based on the decisions made in  $t_2$
  - $t_4$ : a clerk issues or voids the check based on the decision of  $t_3$



# Constraints

- $c_1$ : The two instances of  $t_2$  should be performed by different users
- $c_2$ :  $t_2$  and  $t_3$  should be performed by different users
- $c_3$ :  $t_1$  and  $t_4$  should be performed by different users
- $c_4$ :  $t_2$  must be performed by a role that is more senior than the role that performed  $t_1$  unless  $t_1$  and  $t_2$  are performed by GM
- $c_5$ :  $t_1$  and  $t_2$  must be performed by different users
- $c_6$ : At least three roles should perform the workflow instance



# Constraint Workflow Authorization Scheme

- $(T, \leq, \rho)$ , where  $T$  is a (partially ordered) set of tasks and  $\rho$  is a function from  $T$  to the set of natural numbers indicating the number of occurrences of each task in the workflow
- Role hierarchy:  $(R, \leq)$
- User-role association:  $UA \subseteq U \times R$
- Task-role association:  $PA \subseteq T \times R$
- Constraint-task association:  $PC \subseteq C \times T$
- $R(t) = \{r' \in R : \exists (t, r) \in PA, r' \geq r\}$
- $U(t) = \{u \in U : (u, r) \in UA, r \in R(t)\}$
- Task instance:  $(t_i, u_i, r_i)$
- Workflow instance:  $[(t_1, u_1, r_1), \dots, (t_n, u_n, r_n)]$

Task	Role
$t_1$	$RC$
$t_2$	$RM$
$t_3$	$RM$
$t_4$	$RC$

(c) Task-role assignment relation  $PA$

User	Role
Alice	$RC$
Bob	$RM$
Carol	$RM$
Dave	$RC$
Eve	$GM$
Fred	$TM$

(d) User-role assignment relation  $UA$

# Constraint-Task assignment PC

- $PC \subseteq C \times T$  where  $C = \{c_1, c_2, c_3, c_4, c_5, c_6\}$ 
  - $c_2$ :  $t_2$  and  $t_3$  should be performed by different users
    - $(c_2, t_3) \in PC$
  - $c_1$ : The two instances of  $t_2$  should be performed by different users
    - $(c_1, t_2) \in PC$
  - $c_6$ : At least three roles should perform the workflow instance
    - $(c_6, t_1) \in PC, (c_6, t_2) \in PC, (c_6, t_3) \in PC, (c_6, t_4) \in PC$

# Constraints Specification

## ■ Entailment constraints

- Execution of  $t$  is constrained by the execution of  $t'$  where  $t' < t$
- **Entailed task** of  $t' : t$
- $(ur, t', E, pred)$ 
  - $ur \in \{u, r\}$
  - $E \subseteq U(t')$  if  $ur=u$  or  $E \subseteq R(t')$  if  $ur=r$
  - $pred \in \{=, \neq, <, >, \leqslant, \geqslant\}$
  - $pred(u_{t'}, u_t) = \text{true}$  if  $ur=u$  or  $pred(r_{t'}, r_t) = \text{true}$  if  $ur=r$
- **C<sub>2</sub>**:  $t_2$  and  $t_3$  should be performed by different users
  - $c_2 = (u, t_2, U(t_2), \neq)$

# Cardinality Constraints

- Local cardinality constraints
  - Impose restrictions on the number of users to execute a task
    - **c<sub>1</sub>:** The two instances of t2 should be performed by different users
    - $c_1=(2,2)$
- Global cardinality constraints
  - Impose restrictions on the number of roles to execute a set of tasks
    - **c<sub>6</sub>:** At least three roles should perform the workflow instance
    - $c_6=(T,3)$

# Consistency

- A constrained authorization schema  $((T, \leq, \rho), PA, PC)$  is **sound** if
  - All  $(c, t) \in PC$  is well-formed
    - A constraint-task pair is **well-formed** if
      - E.g.,  $(ur, t', E, pred)$ 
        - $ur = u$  or  $r$
        - $t' < t$
        - $E \subseteq U(t')$  if  $ur = u$  or  $E \subseteq R(t')$  if  $ur = r$
        - $pred \in \{=, \neq, <, >, \leq, \geq\}$
    - For all  $u \in U(t)$  and all  $r \in R(t)$ , there is a successful workflow instance in which  $t$  is executed by  $u$  or  $r$

# Constraint Interaction

- Two constraint-task pairs **interplay** if
  - The constraints are assigned to the same task
    - E.g.,  $((2,2), t_2)$ ,  $((r, t_1, R(t_1), <), t_2)$
  - The constraints are assigned to a task and its entailed task
    - E.g.,  $((u, t', U(t'), \neq), t)$  and  $((2, 2), t')$  where  $t$  is an entailed task of  $t'$
  - The constraints are assigned to a set of restricted tasks in  $T'$ 
    - E.g., for global cardinality constraint  $(T', n_r)$ ,  $((T', n_r), t)$  and  $((T', n_r), t')$  where  $t, t' \in T'$

# Interplaying Sets CT

- Affected tasks in CT
  - $((2,2), t_2), ((r, t_1, R(t_1), <), t_2) : \{t_2\}$
  - $((u, t', U(t'), \neq), t), ((2, 2), t') : \{t\}$
- Non-interplay set SC
  - any  $(c, t)$  in SC does not belong to any CT or they are in some CT but t is not an affected task of that CT
- Any  $(c, t) \in SC$  should be **self-consistent**
- Any CT should be **inter-play-consistent**

# Interplay consistency

- Self-consistent or inter-play consistent
  - Consistency rules for different constraint-task pairs
    - E.g., for  $c=(u, t', E, pred) \in SC$  and  $(c,t) \in PC$ , then for any  $\alpha \in E$ ,  $U(t|t', \alpha, c) \neq \emptyset$  and  $\bigcup_{\alpha \in U(t')} U(t|t', \alpha, c) = U(t)$
    - Computations required
      - Set computation

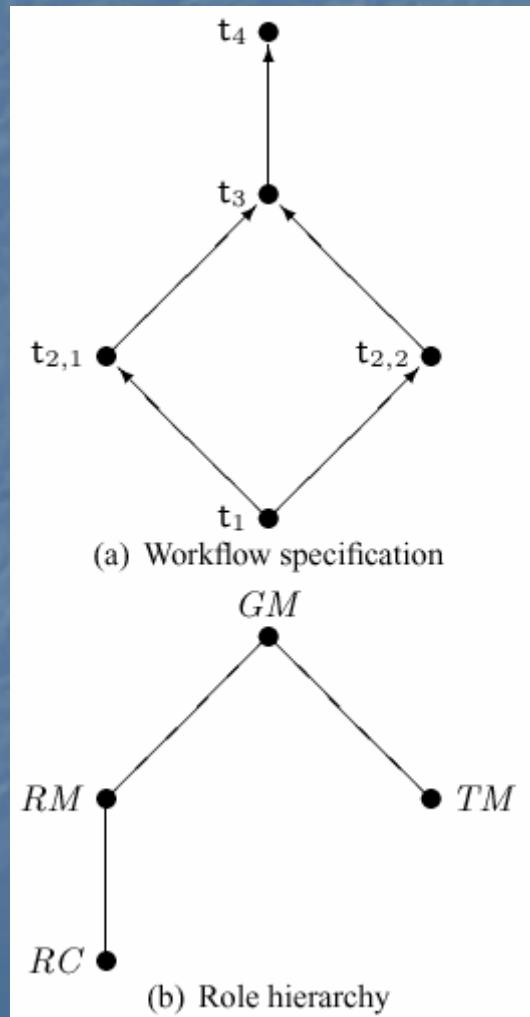
# Main Result

- **Theorem:** a constrained workflow authorization schema  $((T, \leq, \rho), PA, PC)$  is sound if and only if all constraint-task pairs in SC are self-consistent and all the inter-play sets are inter-play-consistent

# Example

- Constraint Inconsistency of our example
  - E.g.  $CT = \{(c_4, t_2), (c_1, t_2)\}$  inter-play
    - $c_1$ : the two instances of  $t_2$  should be performed by different users
      - $c_1 = (2, 2)$
    - $c_4$ :  $t_2$  must be performed by a role that is more senior than the role that performed  $t_1$  unless  $t_1$  and  $t_2$  are performed by GM
      - $c'_4 = (r, t_1, R(t_1), <), c''_4 = (r, t_1, GM, =)$
    - If Bob or Carol executes  $t_1$ , then the workflow instance cannot complete at  $t_2$

# Example



Task	Role
t <sub>1</sub>	RC
t <sub>2</sub>	RM
t <sub>3</sub>	RM
t <sub>4</sub>	RC

(c) Task-role assignment relation *PA*

User	Role
Alice	RC
Bob	RM
Carol	RM
Dave	RC
Eve	GM
Fred	TM

(d) User-role assignment relation *UA*

# Conclusion

- Give explicit definition of constraint workflow authorization schema
- Give a solution to constraints consistency problem in workflow system
  - Simple constraints specification
  - Efficient consistency rules checking