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**Protocol Exploration
With Modern Model Checkers
(I'll be using SAL)**

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Introduction

- It is well-known that bugs in cryptographic protocols can often be found using a **conventional** model checker
 - Build a model of the **protocol**
 - Build a model of the **intruder**
 - Specify some **numbers** of participants, intruders, runs
 - Specify (safety) **properties** of interest
 - **Explore** all reachable states (similar for liveness)
 - Relies on **raw power** to do this
- Cf. specialized **crypto protocol analyzers**
 - Where some of this is built in
 - Used to optimize the search

What's New?

- Modern model checkers offer a variety of **notations**
 - **Hardware** description languages (SMV, BLIF)
 - **Programming** languages (Java, C)
 - Civilized **modeling** languages (SAL)
 - **Intermediate** languages (SAL again)
- They offer several different **tools**
 - **Symbolic, bounded** model checkers (nuSMV)
 - **Explicit-state**, symbolic, bounded, **infinite-bounded**, **witness** model checkers (SAL)
- They are **modular** and **scriptable**
 - Bogor
 - SAL

So What?

- The modeling can be very **direct** at higher levels of abstraction
 - And more **realistic** (e.g., programs) at lower levels
- Easy to model powerful **intruders**
- Can choose the **right tool** for the analysis concerned
 - Have the power to examine the vast number of states generated by powerful intruder models
- **Can model and analyze other parts/properties than security**
- Can do **exploration** as well as model checking

Example: Needham Schroeder

What did you expect?

Message 1. $A \rightarrow B: A.B.\{A, N_A\}_{PK(B)}$

Message 2. $B \rightarrow A: B.A.\{N_A, N_B\}_{PK(A)}$

Message 3. $A \rightarrow B: A.B.\{N_B\}_{PK(B)}$.

I'm going to model and analyze this in SAL

Getting Started: the Network

- Want a “network” that is **generic** wrt. **message type**
- Acts like a one-place buffer
- Messages can be **written** (if empty),
- And **read**, **copied**, **overwritten** (if full)

Network

```
network{msg: TYPE;}: CONTEXT =  
BEGIN  
  bufferstate: TYPE = {empty, full};  
  action: TYPE = {read, write, overwrite, copy};  
  
network: MODULE =  
BEGIN  
  INPUT  act: action, inms: msg  
  OUTPUT nstate: bufferstate, buffer: msg  
INITIALIZATION  
  nstate = empty;  
TRANSITION  
  ...
```

Network (ctd.)

```
[
  act' = write AND nstate = empty -->
    nstate' = full;  buffer' = inms';
[]
  act' = overwrite AND nstate = full -->
    buffer' = inms';
[]
  act' = read AND nstate = full -->
    nstate' = empty;
[]
  act' = copy AND nstate = full -->
    nstate' = nstate;
[]
  ELSE -->
]
```

The Participants

- Need at least two **principals**
- And an **intruder**
- These are **subtypes** of **participants**
- Useful to have an extra “**error**” id for initialization etc.

Participants

```
needhamschroeder: CONTEXT =  
BEGIN  
  ids: TYPE = {a, b, e, X};  
  
  participants: TYPE = {x: ids | x /= X};  
  intruder(x: participants): BOOLEAN = x=e;  
  
  intruders: TYPE = {x: participants | intruder(x)};  
  principals: TYPE = {x: participants | NOT intruder(x)};
```

Nonces

- In **practice**, need to make sure these are fresh
- In **modeling**, they can be deterministic
 - Do not endow the intruder with guessing ability

```
nonces: TYPE = ids;  
nonce(a: participants): nonces = a;
```

Messages

- Messages contain an encrypted component
- When decrypted it's a triple `dmsg`
- `arb` is used for the initial value

```
dmsg: TYPE = [ids, nonces, nonces];  
arb: dmsg = (X,X,X);
```

Otherwise the model checker might use a “magic” value

- An encrypted message records the key used

```
emsg: TYPE = DATATYPE  
  enc(key: ids, payload: dmsg)  
END;
```

- An encrypted message on the network indicates its source and destination

```
msg: TYPE = [# from: participants, to: participants,  
            em: emsg #];
```

- Tuple, datatype, record, just for variety

Decryption

Can successfully decrypt an encrypted message only if you are the participant whose key was used

```
dec(k: participants, m:emsg): dmsg =  
  IF key(m)=k THEN payload(m) ELSE arb ENDIF;
```

Otherwise, get `arb`

State of the Principals

- Initially **sleeping**
- May decide to initiate a dialog and go to **waiting**
- And then to **engaged** if the protocol completes

```
states: TYPE = {sleeping, waiting, engaged,  
                tentative, responding};
```

- If another initiates the dialog, go to **tentative**
- And then to **responding** if the protocol completes
- In either case, **responder** is the identity of the other

Principals

Initially, **each** principal is **sleeping**, and its **responder** is set to itself

```
principal[i: principals]: MODULE =  
BEGIN  
  INPUT nstate: net!bufferstate, imsg: msg  
  GLOBAL act: net!action, omsg: msg  
  LOCAL pc: states, responder: participants  
INITIALIZATION  
  pc = sleeping;  
  responder = i;
```

Principals (ctd. 1)

Waking up and initiating a dialog with j

TRANSITION

```
[  
([] (j: participants): i /= j AND  
  pc = sleeping AND nstate = net!empty -->  
  pc' = waiting;  
  responder' = j;  
  omsg' = (# from := i, to := j,  
           em := enc(j, (i, nonce(i), X)) #);  
  act' = net!write;  
)
```

Principals (ctd. 2)

Waking up and responding to a dialog initiated by **j**

```
[ ]
([ ] (j: participants): i /= j AND
  pc = sleeping AND nstate = net!full
  AND imsg.from = j AND imsg.to = i
  AND dec(i, imsg.em).1=j -->
  responder' = j;
  pc' = tentative;
  act' = net!overwrite;
  omsg' = (# from := i, to := j,
           em := enc(j, (X, dec(i, imsg.em).2, nonce(i))))#);
)
```

Principals (ctd. 3)

Initiator accepts the response from **j**

[]

```
pc = waiting AND nstate = net!full
  AND imsg.from = responder AND imsg.to = i
  AND dec(i,imsg.em).2 = nonce(i) -->
pc' = engaged;
act' = net!overwrite;
omsg' = (# from := i, to := responder,
         em := enc(responder, (X, dec(i,imsg.em).3, X))#);
```

Principals (ctd. 4)

Responder accepts second message from initiator j

```
[ ]
  pc = tentative AND nstate = net!full
    AND imsg.from = responder AND imsg.to = i
    AND dec(i,imsg.em).3 = nonce(i) -->
  pc' = responding;
  act' = net!read;
[ ]
  ELSE -->
]
END;
```

Otherwise do nothing

Intruders

Need to provide the intruder with memory for messages it has seen but not been able to decrypt, and for the contents of messages (i.e., nonces) that it has decrypted

```
intruder[x:intruders]: MODULE =  
BEGIN  
  GLOBAL act: net!action, omsg: msg  
  INPUT nstate: net!bufferstate, imsg: msg  
  LOCAL nmem, n1, n2: nonces, mmem: emsg  
INITIALIZATION  
  nmem = nonce(e);  
  mmem = enc(X, (X, X, X));
```

We provide memory for one of each: **nmem** and **mmem**; **n1** and **n2** are temporaries

Intruders (ctd. 1)

Intruder can read and decrypt messages sent to itself

TRANSITION

```
[  
  nstate = net!full AND imsg.to = x  -->  
  nmem' IN {dec(x,imsg.em).2, nmem};  
  act' IN {net!read, net!copy};
```

Nondeterministically replaces saved nonce with the new one, and removes the message or copies it

Intruders (ctd. 2)

Can save whole messages not addressed to itself

```
[ ]  
  nstate = net!full AND imsg.to /= x -->  
    mmem' IN {imsg.em, mmem};  
    act' IN {net!read, net!copy};
```

Intruders (ctd. 3)

Can send remembered message to j , while masquerading as i

```
[ ]
([ ] (i: participants, j: principals): TRUE -->
  act' = IF nstate = net!empty
    THEN net!write
    ELSE net!overwrite ENDIF;
  omsg' = (# from := i, to := j, em := mem #);
)
```

Intruders (ctd. 4)

And can manufacture messages containing its own nonce or a remembered one

```
[ ]
([ ] (i: participants, j: principals): TRUE -->
  act' = IF nstate = net!empty
    THEN net!write
    ELSE net!overwrite ENDIF;
  n1' IN {nmem, nonce(x)};    n2' IN {nmem, nonce(x)};
  omsg' = (# from := i, to := j, em := enc(j, (i, n1', n2'))#);
)
[ ]
  ELSE -->
]
END;
```

And that's all it can do

The Complete System

- **Asynchronously** compose some collection of principals and intruders
 - And **synchronously** compose that compound with the network
 - We'll have two principals **a** and **b**, and single intruder **e**
- No explicit limit on interleaved runs

```
system: MODULE =  
  (([] (id: principals): principal[id]) [] intruder[e])  
  || (RENAME buffer TO imsg, inms TO omsg IN net!network);
```

- We rename the **buffer** and **inms** of the network so that they connect up to the **imsg** and **omsg** of the principals and intruder

Authentication Property

- The property we wish to examine is correct authentication
- Whenever a principal **x** reaches the **responding** state with a principal **y**, must be that **y** initiated the protocol with **x**
 - That is, **y** must be in the **waiting** or **engaged** states and have **x** as its responder
- We specify this as the property **prop**

```
prop: THEOREM system |- G((FORALL (x,y: principals):  
  (pc[x]=responding AND responder[x]=y) =>  
    ((pc[y]=waiting OR pc[y]=engaged)  
     AND responder[y]=x)));
```

Model Checking

- Symbolic model checking

- `sal-smc -v 3 needhamschroeder prop`

Builds a transition relation on 150 state bits, 339,917,146 reachable states, and reports a counterexample ten steps long in about 20 secs

- Witness model checking

- `sal-wmc -v 3 needhamschroeder prop`

Also reports the counterexample, in about 40 secs

- Bounded model checking

- `sal-bmc -v 3 -d 10 needhamschroeder prop`

Builds a SAT problem with 40,756 nodes and reports the counterexample in about 40 secs

The Counterexample

Step 0: Initialization

Step 1: a sends message 1 to e

```
pc[a] = waiting; pc[b] = sleeping; responder[a] = e;
ormsg.from = a; ormsg.to = e; ormsg.em = enc(e, (a, a, X));
```

Step 2: e remembers a's nonce: nmem = a;

Step 3: e (masquerading as a) send message 1 to b

```
ormsg.from = a; ormsg.to = b; ormsg.em = enc(b, (a, a, a));
```

Step 4: b sends message 2 to a, but it is intercepted by e

```
pc[a] = waiting; pc[b] = tentative; responder[b] = a;
ormsg.from = b; ormsg.to = a; ormsg.em = enc(a, (X, a, b));
```

Step 5: e remembers encrypted part of b's message

```
mmem = enc(a, (X, a, b));
```

Step 6: e sends message 2 (using remembered part) to a

```
ormsg.from = e; ormsg.to = a; ormsg.em = enc(a, (X, a, b));
```

Step 7: a sends message 3 to e

```
pc[a] = engaged; pc[b] = tentative;
ormsg.from = a; ormsg.to = e; ormsg.em = enc(e, (X, b, X));
```

Step 8: e remembers b's nonce from a's message 3: nmem = b;

Step 9: e (masquerading as a) sends message 3 to b (with remembered nonce)

```
ormsg.from = a; ormsg.to = b; ormsg.em = enc(b, (a, e, b));
```

Step 10: b falsely believes it has authenticated a: pc[b] = responding;

The Counterexample (ctd.)

Is essentially the classic one

Message 1a. $A \rightarrow I: A.I.\{A, N_A\}_{PK(I)}$

Message 1b. $I_A \rightarrow B: A.B.\{A, N_A\}_{PK(B)}$

Message 2b. $B \rightarrow I_A: B.A.\{N_A, N_B\}_{PK(A)}$

Message 2a. $I \rightarrow A: I.A.\{N_A, N_B\}_{PK(A)}$

Message 3a. $A \rightarrow I: A.I.\{N_B\}_{PK(I)}$

Message 3b. $I_A \rightarrow B: A.B.\{N_B\}_{PK(B)}$.

Here, I_A indicates I masquerading as A , and the suffices a, and b on the message numbers indicate which run of the protocol they belong to

Repairing The Protocol

The protocol is easily fixed by including the identity of the responder in the encrypted portion of the second message (this prevents the replay of the encrypted portion of 2b in 2a)

Message 2'. $B \rightarrow A: B.A.\{B, N_A, N_B\}_{PK(A)}$

Repairing The Protocol (ctd.)

- In SAL, we need to change the final assignment on slide 17 to the following (the **X** is changed to **i**)

```
omsg' = (# from := i, to := j,  
         em := enc(j, (i, dec(i,imsg.em).2, nonce(i))))#);
```

- The guard on slide 18 must then be changed (by addition of the third line below) to check that the message really does come from the expected responder

```
pc = waiting AND nstate = net!full  
AND imsg.from = responder AND imsg.to = i  
AND dec(i,imsg.em).1 = responder  
AND dec(i,imsg.em).2 = nonce(i) -->
```

Model Checking Again

- Symbolic model checking

- `sal-smc -v 3 needhamschroeder prop`

This time there are **339,954,654** reachable states, and the property is “verified” in 25 seconds

- Verification is relative to the intruder model and dimensions used

- Witness model checking

- `sal-wmc -v 3 needhamschroeder prop`

Verifies the property in 30 seconds, and (internally) constructs a **witness**

- Bounded model checking

- `sal-bmc -v 3 -d 10 needhamschroeder prop`

Finds no counterexamples to depth 10 in 85 seconds

Exploration

- Finding bugs and verifying are extreme examples of **exploration**
- In general, want to see runs that take us to interesting states or through interesting scenarios as a way of increasing our understanding and confidence in the operation of the system
- Can do this in a simulator, but have to think of all the inputs and interactions ourselves
- **Supposing we had a simulator built on a model checker**
- Then we could tell the model checker to find a path to an interesting state, then take over and explore in detail, and so on
- The **SAL simulator** does this

Exploration with the SAL Simulator

- Suppose we are interested in the scenario where the intruder spoofs both principals into thinking they are responding to the other
- We start the simulator and tell it to take us to a state where both principals are in **tentative** state

```
tulip:sal> sal-sim
SAL Simulator (Version 2.2). Copyright (c) 2003, 2004 SRI
sal > (import! "needhamschroeder")
sal > (start-simulation! "system")
sal > (run! "(and (= pc[a] tentative) (= pc[b] tentative))")
#t
```

- The **#t** means it succeeded
- Notice we're using **LSAL** syntax here

Exploration with the SAL Simulator (ctd. 1)

- Now we would like to see the intruder continue and bring both principals to the **responding** state

```
sal > (run! "(and (= pc[a] responding) (= pc[b] responding))")
#f
```

- The **#f** means it failed
- Perplexed, we see if it can bring either to completion

```
sal > (run! "(or (= pc[a] responding) (= pc[b] responding))")
#f
```

- Hmm! Let's restart and find a path where **a** is responding to the intruder

```
sal > (start-simulation! "system")
sal > (run! "(and (= pc[a] responding) (= responder[a] e))")
#f
```

Exploration with the SAL Simulator (ctd. 1)

- So let's get to a state where **a** is in the **tentative** state (which we already know is possible)

```
sal > (run! "(and (= pc[a] tentative) (= responder[a] e))")
#t
```

- Now we know that the intruder should be able to construct the message to take **a** to the **responding** state provided it knows **a**'s nonce (which is also **a**)
- So let's see if the intruder does know this nonce in the current state

```
sal > (filter-curr-states! "(= nmem a)")
sal > (display-curr-states)
#t
```

Evidently not—the **#t** means the filtered set is empty (we also could have just looked at the current state)

Exploration with the SAL Simulator (ctd. 2)

- So now let's get back to where we were

```
sal > (backtrack!)
sal > (run! "(and (= pc[a] tentative) (= responder[a] e))")
#t
```

- And look for a state where the intruder knows the nonce

```
sal > (run! "(= nmem a)")
#f
```

- Hmm! Let's go back to the beginning and look for **any** state where it knows this nonce

```
sal > (start-simulation! "system")
sal > (run! "(= nmem a)")
#t
sal > (display-curr-states)
```

Exploration with the SAL Simulator (ctd. 3)

- It turns out the simulator has found a run where **a** initiated the dialog
- It seems that the intruder can learn **a**'s nonce when **a** is the initiator, but not when it is the responder
- The difference between these cases is that **a**'s nonce is in the second position of the **emsg** tuple in the former case, and the third in the latter
- Sure enough, the command in the relevant step of the intruder is the following

```
nmem' IN {dec(x,imsg.em).2, nmem}
```

It should, of course, be changed as follows

```
nmem' IN {dec(x,imsg.em).2, dec(x,imsg.em).3, nmem}
```

Exploration with the SAL Simulator (ctd. 3)

- After making this change, we exit the simulator and restart it, and again check the properties of interest

```
sal > (import! "needhamschroeder")
sal > (start-simulation! "system")
sal > (run! "(and (=pc[a] responding) (=responder[a] e))")
#t
sal > (run! "(and (=pc[a] responding) (=pc[b] responding))")
#t
```

This time, the simulator is able to find suitable paths

- We also check that the authentication property is still true using [sal-smc](#)

Summary

- Modern model checkers are attractive and effective tools for exploring protocols
- Can add GUIs and also raise modeling level
- For example, Guido Wimmel at TUM models e-commerce protocols in the Focus graphical environment
 - Messages are specified as **secret**, **authentic**, etc.
 - A suitable intruder model is synthesized
 - Properties are selected
 - And the whole lot sent to a model checker

Summary (ctd.)

- A simulation environment built on a model checker provides a powerful environment for **exploring** protocols
- The **sal-sim** environment is **scriptable** in Scheme
- **In fact, the SAL model checkers are just Scheme scripts on the underlying API**
- Can develop **novel capabilities** as scripts on this API
 - Example: test case generation
- See fm.csl.sri.com for our tools
- <http://www.csl.sri.com/users/rushby/abstracts/needham03> for this example

Putting More Things Together

- It is now fairly routine to have model checkers as backends to theorem provers (e.g., PVS), or proof assistants as front ends to model checkers (e.g., Cadence SMV)
 - **But we envisage a larger collection of symbolic computational procedures**
 - Decision procs, ITPs, abstractors, inv generators, model checkers, static analyzers, test generators, ITPs, rewriters
 - **Interacting** through a **scriptable tool bus**
 - The bus manages symbolic and concrete **artifacts**
 - Test cases, abstractions, theorems, invariants
- Over which it performs **evidence management**
- Focus shifts from verification to **symbolic analysis**
 - **Iterative application of analysis to artifacts to yield new artifacts, insight and evidence**

Integrated, Iterated Analysis

